

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r^2} \hat{r}$$

$$\vec{F}_2 = q_2 \vec{E}_1$$

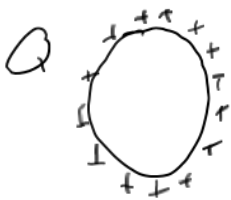


$$|\vec{E}_{axis}| \approx \frac{1}{4\pi\epsilon_0} \frac{2qs}{r^3}$$

$$|\vec{E}_\perp| \approx \frac{1}{4\pi\epsilon_0} \frac{qs}{r^3}$$

$r \gg s$

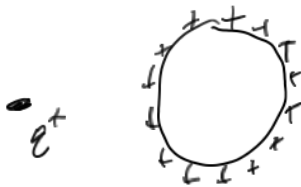
$$\rho = 0$$



uniform shell of charge

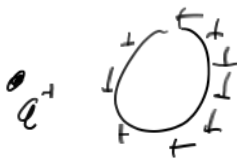
$\vec{E}_{\text{inside}}$ due to charges on the shell is 0

$E_{\text{outside}} \quad \vec{E} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \hat{r}$

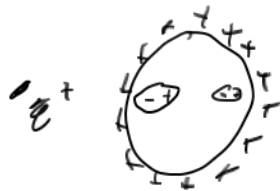


conductor $\rightarrow \vec{E}_{\text{inside}} = 0$

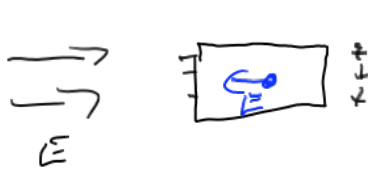
insulator $\rightarrow E_{\text{inside}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \hat{r}$

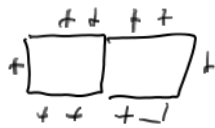


conductor

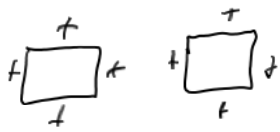


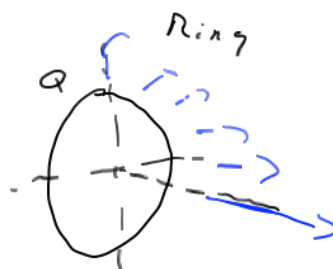
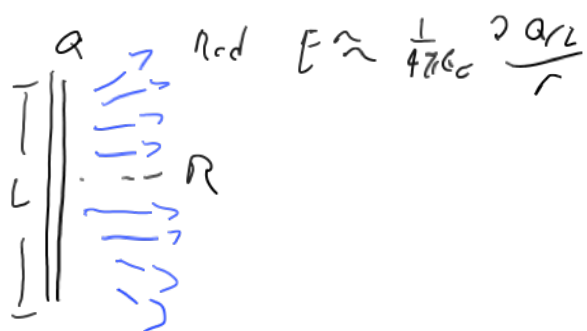
$E_{\text{inside}} = \frac{E_{\text{app}}}{K}$


 $\times \quad \mathcal{E}_{tot} = \mathcal{E} + \mathcal{E}_- + \mathcal{E}_+$

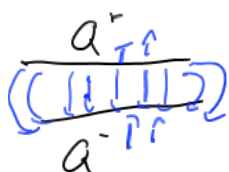


conservation of charge





$$E \approx \frac{Q/A}{\epsilon_0}$$



Capacitor
 $E_{cap} \approx \frac{Q/A}{\epsilon_0}$

$$\Delta V = V_f - V_i = - \int_i^f \vec{E} \cdot d\vec{l} \quad \text{if } \vec{E} \text{ is constant}$$

$$\rightarrow \Sigma = E \cdot \Delta l$$



$$\text{if } \vec{E} \text{ and } d\vec{l} \text{ are } \perp \rightarrow \Delta V = 0$$

$$\Delta U = q \Delta V$$

$$\text{round trip } \Delta V = 0$$

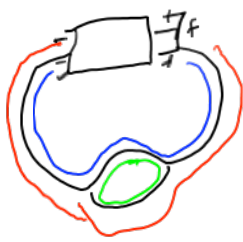
$$\vec{B} = \frac{\mu_0}{4\pi} \oint \frac{\vec{v} \times \hat{r}}{r^2}$$

$$\begin{aligned} \vec{v} \times \hat{r} &= |\vec{v}| |\hat{r}| \sin \theta \\ &= |\vec{v}| \sin \theta \end{aligned}$$

$$\Delta \vec{B} = \frac{\mu_0}{4\pi} \frac{I \Delta \vec{d} \times \hat{r}}{r^2}$$



$$\mu = A I$$



current node

$$i_{in} \sim i_{out} \rightarrow I_{in} = I_{out}$$

$\mathcal{E}_{if}$ or Energy Conservation

$$\Delta V = 0$$

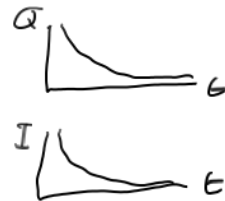
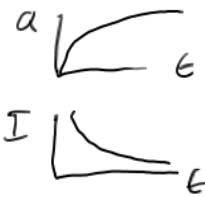
$$\mathcal{E}_{mf} - I_1 R_1 + \dots = 0$$

$$I = |q| n A v E$$

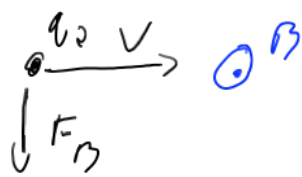
$$R = \frac{L}{\sigma A}$$

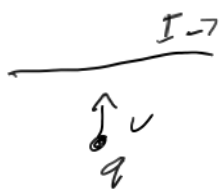
$$\sigma = |q| n v$$

$$\Delta V = IR \text{ ohmic only!}$$

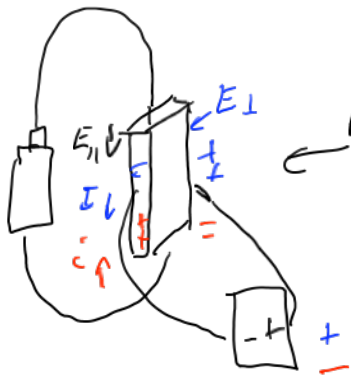


$q_0 \vec{v} \rightarrow \odot \vec{B}$
 $\vec{F}_0 = q_0 \vec{E}_1 + q_0 \vec{v}_0 \times \vec{B}_1$

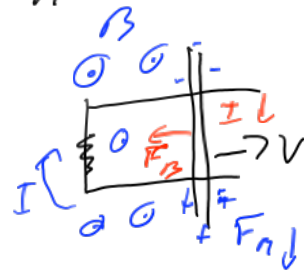




~~$F_0 = q_0 \vec{v}_0 \times (\vec{v}_0 \times \vec{r}) \frac{\mu_0}{4\pi}$~~



$F_B = F_{E\perp}$
 $q v B = q E_{\perp}$



$$\Phi = \oint \vec{E} \cdot \hat{n} d\alpha = \frac{\sum q_{in}}{\epsilon_0} \quad \oint \vec{B} \cdot \hat{n} d\alpha = 0$$



all of these charges
contribute to the field
of the surface!

but only q_{in} contributes
to flux

Gauss' Law

Ampere's Law

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 \sum I_{in}$$



direction of $d\vec{l}$
is arbitrary



$$\mathcal{E}_{mf} = - \frac{d\Phi}{dt}$$

$$\mathcal{B}_s = \frac{\mu \cdot N I}{d}$$

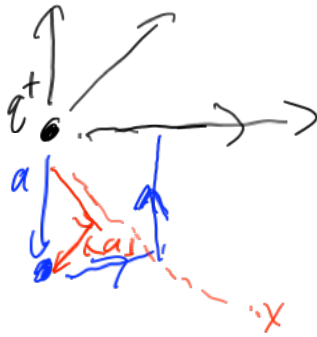
$$\Phi = \int \vec{B} \cdot \hat{n} da$$

$$\Phi_{rw} = \Phi_{rs} \rightarrow \frac{d\Phi_{rw}}{dt} = \frac{d\Phi_{rs}}{dt}$$

$$\frac{d\mathcal{E}}{dt} = \frac{\mu \cdot N}{d} \pi r_s^2 \frac{dI}{dt} = 0.016 V = \mathcal{E}_{mf}$$

$$\mathcal{E}_{mf} = \oint \vec{E}_{nc} \cdot d\vec{l} \rightarrow \mathcal{E}_{mf} = E_{nc} \int \pi r_w$$

$$E_{nc} = \frac{\mathcal{E}_{mf}}{\int \pi r_w} = .0035 \frac{V}{m}$$



$$a_{\perp} = a$$

x

$$E_{\text{rad}} = \frac{1}{4\pi\epsilon_0} \frac{q a_{\perp}}{c^2 r} \quad a_{\perp, r} \text{ from observer}$$

$$a_{\perp}^x = 0$$

$$\vec{B} = \hat{E} \times \hat{B}$$

$$|\vec{E}| = |\vec{B}| c$$

$$\rightarrow |\vec{B}| = \frac{|\vec{E}|}{c}$$